# Average Trends over Millennia of Evolution Supervised by Genetic Algorithms. Analysis of Phenotypes 

Lorentz JÄNTSCHI ${ }^{1)}$, Sorana D. BOLBOACǍ ${ }^{2}$, Mircea V. DIUDEA ${ }^{3)}$, Radu E. SESTRAȘ ${ }^{4)}$<br>${ }^{1}$ Technical University of Cluj-Napoca, Department of Chemistry, 103-105 Muncii Bvd., 400641 Cluj-Napoca, Romania; lori@academicdirect.org<br>2 "Iuliu Hațieganu" University of Medicine and Pharmacy Cluj-Napoca, Department of Medical Informatics and Biostatistics, 6 Louis Pasteur, 400349 Cluj-Napoca, Romania; sbolboaca@umfcluj.ro<br>${ }^{3}$ Babeş Bolyai University, Faculty of Chemistry and Chemical Engineering, Arany Janos no. 11, 400028 Cluj-Napoca, Romania; diudea@chem.ubbcluj.ro<br>${ }^{4}$ University of Agricultural Sciences and Veterinary Medicine Cluj-Napoca, 3-5 Mănăştur, 400372 Cluj-Napoca, Romania; rsestras@usamvcluj.ro


#### Abstract

A genetic algorithm (GA) had been developed and implemented in order to identify the optimal solution in term of determination coefficient and estimation power of a multiple linear regression approach on structure-activity relationships. The Molecular Descriptors Family was used for structure characterization of a sample of 206 polychlorinated biphenyls with measured octanol-water partition coefficients as case study. The research aimed to analyze the degree of association between the number of viable genotypes in cultivar in generations when the evolution occurred and the selection and survival strategies. The GA was run by 46 times and the Anderson-Darling test was used to compared the distribution laws of populations occurred by using different pairs of survival and selection strategies. The records of genotypes number were analyzed and the conclusions were highlighted.


Keywords: Anderson-Darling Test, Genetic Algorithm (GA), Distribution; Phenotypes.

## INTRODUCTION

Genetic algorithms (GAs) are search and optimization methods inspired from process of natural evolution (Fraser, 1957a; 1957b). Besides their usefulness in finding solutions of hard problems of decision (Juan et al., 2010), classification (Duval and Hao, 2009), optimization (Di Serafino et al., 2010), and simulation (Stamatakis and Zygourakis, 2010), the GAs are also used in optimization quantitative structure-activity relationships - qSAR - (Ghosh and Bagchi, 2009) as well as in drug discovery (Teixidó et al., 2005).

The main researches in using the genetic algorithm for qSAR/qSPR (quantitative StructureProperty Relationships) investigations deal with variable selection (Wu et al., 2010), optimization (Jäntschi et al., 2010a), model identification (Dashtbozorgi and Golmohammadi, 2010), identification of best design of experiment (Yang et al., 2010), in silico screening (Hemmateenejad et al., 2010), etc. Despite of the interest in using the GAs in qSAR/qSPR, there are just few articles which present the assessment of the GA in terms of viable genotypes and phenotypes in cultivar. Our present research was focus on finding the answer to the question "Is the average number of viable phenotypes in cultivar dependent or not by the selection and survival strategies?"

## MATERIAL AND METHODS

An analysis of structure-activity relationships was carried out on a sample of 206 PCBs (with octanol-water partition coefficients (Eisler and Belisle, 1996) expressed in logarithmic scale $\left(\ln \left(\mathrm{K}_{\text {ow }}\right)\right)$ as property of interest) using a home-made genetic algorithm (Jäntschi, 2010b; Jäntschi et al., 2010c; Jäntschi et al., 2010d). The molecular descriptors family (MDF) approach (Jäntschi, 2004) was used to link the structure of the PCBs to the octanol-water partition coefficients. The GA experiment was repeated by 46 times and a series of parameters has been counting during the evolution of the heuristics; the number of viable phenotypes (sum_obs), average of viable phenotypes (avg_obs) according to GA evolution were of interest for the present research.

A program to analyze the distribution of the pair sampling using the Anderson-Darling test (Anderson and Darling, 1952) was develop and implemented in order to answer the research question. Anderson-Darling test verify if there is a statistical evidence that a sample is from a given probability function. Details about the formulas applied are detailed in (Jäntschi et al., 2010e).

## RESULTS AND DISCUSSION

The summary of the number of viable phenotypes expressed as means on thousand of generations (from $0 . .1000$ to 1901..20000) according to each pair of selection and survival strategy is presented in Tab. 1.

Tab. 1
Frequency of viable phenotypes in cultivar (cumulated from 46 experiments) when evolution occurred for each pair of selection and survival strategies

|  | 1000G | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | avg_obs | 17 | 17.9 | 17.3 | 17.8 | 17.9 | 18.2 | 19.2 | 17.9 | 17.4 | 17.9 | 19.6 | 18.1 | 18.0 | 17.5 | 17.9 | 18.0 | 19.1 | 19.0 | 19 | 18.9 |
|  | sum_obs | 1311 | 252 | 167 | 110 | 643 | 799 | 479 | 537 | 610 | 573 | 567 | 289 | 360 | 262 | 143 | 126 | 229 | 400 | 330 | 77 |
| PT | avg_obs | 18.2 | 18.5 | 18.5 | 19.8 | 20.7 | 19.3 | 19.0 | 19.3 | 17.2 | 18.0 | 18.8 | 18. | 18 | 15. | 17. | 18 | 16.5 | 17 | 16 | 14.6 |
|  | sum_obs | 1296 | 315 | 24 | 17 | 111 | 851 | 758 | 636 | 551 | 576 | 207 | 508 | 592 | 414 | 177 | 385 | 99 | 140 | 76 | 219 |
| PD | avg_ob | 18.1 | 17.7 | 18. | 17.7 | 17 | 18. | 17. | 18.4 | 18.1 | 18. | 17.7 | 17 | 18 | 18. | 16. | 17. | 18 | 17 | 17 | 15.8 |
|  | sum_obs | 1354 | 2809 | 18 | 150 | 1046 | 1315 | 413 | 461 | 507 | 381 | 389 | 570 | 445 | 449 | 160 | 261 | 284 | 377 | 245 | 85 |
| TP | avg_ob | 18.0 | 18 | 18 | 19. | 19 | 19.2 | 18.0 | 18.6 | 19.8 | 19.0 | 19. | 19. | 18. | 20. | 18 | 19. | 17 | 18 | 18 | 19. |
|  | sum_obs | 11766 | 63004 | 2077 | 1692 | 1106 | 594 | 666 | 614 | 674 | 514 | 489 | 436 | 317 | 184 | 130 | 157 | 161 | 217 | 185 | 252 |
| TT | avg_ob | 18.5 | 18. | 17 | 17 | 18 | 18.1 | 19.1 | 18. | 19.3 | 18.6 | 18.8 | 17.7 | 18. | 19 | 18 | 18 | 18 | 19 | 19 | 17.4 |
|  | sum_obs | 13681 | 325 | 164 | 111 | 1021 | 671 | 726 | 587 | 406 | 427 | 358 | 443 | 254 | 323 | 340 | 456 | 163 | 19 | 139 | 209 |
| TD | avg_ob | 18.1 | 18.5 | 18. | 18 | 18 | 18.2 | 18.0 | 18.0 | 18.2 | 18.6 | 19.1 | 20.0 | 17.9 | 17. | 20 | 19. | 17. | 18 | 17 | 17.1 |
|  | sum_ob | 1371 | 2037 | 1762 | 152 | 113 | 1200 | 883 | 703 | 382 | 576 | 553 | 500 | 556 | 284 | 102 | 76 | 24 | 165 | 195 | 274 |
| DP | avg_obs | 16.2 | 15.1 | 14.6 | 15.7 | 15.7 | 14.6 | 13.9 | 14.3 | 14.7 | 15.4 | 16.7 | 16.2 | 14. | 12 | 14 | 16.4 | 14 | 15 | 15 | 17.8 |
|  | sum_obs | 6817 | 1418 | 642 | 518 | 676 | 409 | 209 | 613 | 457 | 231 | 251 | 276 | 174 | 215 | 233 | 148 | 213 | 263 | 95 | 89 |
| DT | avg_obs | 16.3 | 15.5 | 15.3 | 15.3 | 15.5 | 15.6 | 15.4 | 14.3 | 14.9 | 15.5 | 13.8 | 14.0 | 15.2 | 15. | 16. | 14.7 | 15. | 15. | 15.2 | 12 |
|  | sum_obs | 7044 | 170 | 996 | 780 | 745 | 609 | 585 | 643 | 538 | 665 | 193 | 351 | 441 | 200 | 131 | 235 | 121 | 156 | 167 | 25 |
| DD | avg_obs | 17.8 | 18.2 | 19.1 | 18.1 | 18.3 | 17.3 | 17.7 | 18.4 | 19.9 | 18.6 | 17.7 | 19.2 | 19.6 | 17.8 | 19.0 | 17.9 | 17.4 | 19.5 | 17.6 | 16. |
|  | sum_obs | 8284 | 218 | 15 | 119 | 969 | 711 | 424 | 717 | 1015 | 446 | 195 | 364 | 352 | 409 | 436 | 250 | 330 | 234 | 423 | 33 |

Sel = selection strategy; Srv = survival strategy; avg_obs = mean of observations; sum_obs = sum of observations; 1000G = thousands of generations; P = proportional; $\mathrm{T}=$ tournament; $\mathrm{D}=$ deterministic

Anderson-Darling test has been applied in order to accomplish the aim of the research by investigation of a total number of 502 cases. The smallest value of Anderson-Darling statistics of 0.6096 was observed when the following pairs of selection and survival strategies were analyzed: PT (proportional selection accompanied by tournament survival) and DD (deterministic selection accompanied by deterministic survival). The highest value of Anderson-Darling statistics of 15.6013 was observed when the following pairs of selection and survival strategies were analyzed:

PP (proportional selection accompanied by proportional survival) and DT (deterministic selection accompanied by tournament survival). In $7 \%$ of investigated cases the hypothesis that the groups are from identical population could not be rejected at a significance level of $5 \%$. In $93 \%$ of cases, with a $5 \%$ risk to be in error, it could be stated that the investigated groups of selection and survival strategies are from different populations. Moreover, the population interpretation of the average number of viable phenotypes in cultivar in generation when evolution occurred is more complex compared to the population interpretation of the number of genotypes.

The interpretation of the results requires the identification of the largest group of pairs of methods with possible identical populations (hereafter named list of suspects - suspected to originate from the population with identical distributions) and elimination of their unique subgroups of inferior order. Thus, the groups of higher order are group of order 5 (PP, PT, TT, TD, DD) - run 400 - and (PP, PT, PD, TD, DD) - run 448 - that automatically enter in the list of suspects; the inferior order groups are as it results from application of the inclusion algorithm:
$\div$ Groups of $5^{\text {th }}$ order; list of suspects: $\{(\mathrm{PP}, \mathrm{PT}, \mathrm{TT}, \mathrm{TD}, \mathrm{DD})$, (PP, PT, PD, TD, DD) $;$; (PP, PT, TD, DD) - run 384 - is simultaneously in (PP, PT, TT, TD, DD) and (PP, PT, PD, TD, DD) making it impossible to detect its membership, is it added to the list of suspects; ■ (PT, TT, TD, DD) - run 145 - is just in (PP, PT, TT, TD, DD); is deleted; ■ (PP, TT, TD, DD) - run 272 - is just in (PP, PT, TT, TD, DD); is deleted; - (PP, PT, TT, DD) - run 392 - is just in (PP, PT, TT, TD, DD); is deleted; ( (PP, PT, TT, TD) - run 399 - is just in (PP, PT, TT, TD, DD); is deleted; ■ (PP, PT, PD, DD) - run 440 - is just in (PP, PT, PD, TD, DD); is deleted; ■ (PT, PD, TD, DD) - run 193 - is just in (PP, PT, PD, TD, DD); is deleted; ( $\quad$ (PP, PT, PD, TD) - run 447 - is just in (PP, PT, PD, TD, DD); is deleted;
$\div$ Groups of at least $4^{\text {th }}$ order; list of suspects: \{(PP, PT, TT, TD, DD), (PP, PT, PD, TD, DD), (PP, PT, TD, DD) \}: ■ (PT, TD, DD) - run 129, (PP, PT, DD) - run 376, (PP, TD, DD) - run 256, (PP, PT, TD) - are simultaneously in (PP, PT, TT, TD, DD), (PP, PT, PD, TD, DD) and (PP, PT, TD, DD); are added; ■ (TT, TD, DD) - run 20, (PT, TT, TD) - run 144, (PT, TT, DD) run 137, (PP, TT, TD) - run 271, (PP, TT, DD) - run 264 and (PP, PT, TT) - run 391 - are just in (PP, PT, TT, TD, DD); are deleted; ■ (PT, PD, DD) - run 185, (PP, PT, PD) - run 439 and (PP, $\mathrm{PD}, \mathrm{DD}$ ) - run 312 - are just in (PP, PT, PD, TD, DD); are deleted;
$\div$ Groups of at least $3^{\text {rd }}$ order; list of suspects: \{(PP, PT, TT, TD, DD), (PP, PT, PD, TD, DD), (PP, PT, TD, DD), (PT, TD, DD), (PP, PT, DD), (PP, TD, DD), (PP, PT, TD) $: ~ ■ ~(P T, ~ D D) ~-~$ run 121 - is in runs 376, 129, 384, 448, 400; is added; ■ (TT, TD) - run 19, (PT, TT) - run 136, (TT, DD) - run 12, (PP, TT) - run 263 - in run 400; are deleted; - (PP, DD) - run 248 - in runs $256,376,384,448,400$; is added; $\quad$ (TD, DD) - run 5 - in runs 256, 129, 384, 448 and 400 ; is added; ■ (PT, TD) - run 128 - in runs 383, 129, 384, 448 and 400; is added; ■ (PP, TD) - run 255 - in runs 383, 256, 384, 448 and 400; is added; (DP, DT) - run 3 - is not found in the higher-order groups; is added; ■ (PP, PT) - run 375 - in run $383,376,384,448,400$; is added; ■ (PT, PD) - run 184 and (PD, DD) - in run 448; are deleted; (TP, TT) - run 42 - is not found in the higher-order groups; has the highest susceptibility being closest to the 95 confidence for rejection (c/k=1.09); is deleted.
$\div$ Groups of at least $2^{\text {nd }}$ order; list of suspects: \{(PP, PT, TT, TD, DD), (PP, PT, PD, TD, DD), (PP, PT, TD, DD), (PT, TD, DD), (PP, PT, DD), (PP, TD, DD), (PP, PT, TD), (PT, DD), (PP, DD ), (TD, DD), (PT, TD), (PP, TD), (DP, DT), (PP, PT)\}; it is imposed to continue the inclusion in the list of distinct populations by following the previous procedure: $■$ PP is found in several groups of higher order; is added; ■ PT is found in several groups of higher order; is added; ■ PD is found in just one group of higher order (PP, PT, PD, TD, DD); is deleted; ■ TP is not found in any group of higher order; is added; ■ TT is found in just one group of higher order: (PP, PT, TT, TD, DD); is deleted; ■ TD is found in several groups of higher order; is
added; ■ DP is found in just one group of higher order: (DP, DT); is deleted; ■ DT is found in just one group of higher order: (DP, DT); is deleted; ■ DD is found in several groups of higher order; is added;
$\div$ All distinct groups; final list: \{(PP, PT, TT, TD, DD), (PP, PT, PD, TD, DD), (PP, PT, TD, DD), (PT, TD, DD), (PP, PT, DD), (PP, TD, DD), (PP, PT, TD), (PT, DD), (PP, DD), (TD, DD), (PT, TD), (PP, TD), (DP, DT), (PP, PT), PP, PT, TP, TD, DD\};

The list of possible phenotypes populations with the associated level of confidence can now be constructed and is presented in Tab. 2 (the classification is according to the obtained level of confidence).

Tab. 2
Number of phenotypes in cultivar during evolutions: populations parameterized by selection and survival having distinct distribution laws

| Population | $\mathrm{M}(\mathrm{c} / \mathrm{k})$ [n_obs] | Cat | Interpretation and the significance level |
| :---: | :---: | :---: | :---: |
| (DP, DT) | 0.194 [128] | 1 | With a 5\% risk of being in error produce a population different by all other pairs of methods. |
| TP | 0.293 [255] |  |  |
| (PP, PT, PD, TD, DD) | 0.368 [16] | 2 | The hypothesis of come from the same population could not be rejected (at a 95\% confidence) |
| (PP, PT, TT, TD, DD) | 0.409 [16] |  |  |
| PP | 0.390 [255] | 3.1 | The hypothesis of identical distribution with more populations could not be rejected (at a 95\% confidence) |
| TD | 0.405 [255] |  |  |
| DD | 0.417 [255] |  |  |
| PT | 0.417 [255] |  |  |
| (PP, TD) | 0.400 [128] | 3.2 | The hypothesis of identical distribution with more populations could not be rejected (at a 95\% confidence) |
| (PP, PT) | 0.407 [128] |  |  |
| (PP, DD) | 0.417 [128] |  |  |
| (PT, TD) | 0.419 [128] |  |  |
| (TD, DD) | 0.419 [128] |  |  |
| (PT, DD) | 0.444 [128] |  |  |
| (PP, PT, TD) | 0.407 [64] | 3.3 | The hypothesis of identical distribution with more populations could not be rejected (at a 95\% confidence) |
| (PP, TD, DD) | 0.413 [64] |  |  |
| (PP, PT, DD) | 0.424 [64] |  |  |
| (PT, TD, DD) | 0.430 [64] |  |  |
| (PP, PT, TD, DD) | 0.422 [32] | 3.4 | The hypothesis of identical distribution with more populations could not be rejected (at a 95\% confidence) |

$\mathrm{M}(\mathrm{c} / \mathrm{k})$ [n_obs] - Mean of $\mathrm{c} / \mathrm{k}$ (number of observations in calculation of the mean); Cat = category
Remark: the smallest mean of $c / k$, the better relevance in the interpretation;
The $\mathrm{c} / \mathrm{k}$ higher than 1 attract the susceptibility of interpretation rejection;
The analysis of results presented in Tab. 2 give us the possibility to statistically separate the populations. Thus, the $1^{\text {st }}$ category of significance contains populations identified as distinct versus other populations (Fig. 1 - mean values on intervals of thousand generations; Fig. 2 - mean tendencies on intervals of thousand generations).

The analysis of Fig. 1 and 2 showed that the average number of phenotypes is different not only by the mean distribution law on evolutions (as it can be observed from Tab. 1) but also in terms of absolute value of the average number of phenotypes in cultivar.

Tournament selection associated to proportional survival (TP) produce a population of distinct phenotypes in cultivar in terms of their number (its mean is situated above the mean produced by remaining methods - PP, PT, PD, TT, TD, DD - in all moments of evolution - see Fig. 1). Moreover, the mean of phenotypes number obtained by applying the tournament selection and proportional survival systematically increase with almost one phenotype compared with all other methods (mean of 18.94 for TP; mean of 18.18 for $\mathrm{PP}+\mathrm{PT}+\mathrm{PD}+\mathrm{TT}+\mathrm{TD}+\mathrm{DD}$ ) and in all cases with more than one phenotype compared to overall mean (17.59), having the increasing tendency19 to
phenotypes during evolution (Fig. 2).


Fig. 1. Segregation of the populations of average number of viable phenotypes in the moments of evolution; populations: (DP and DT), TP and the rest of selection and survival strategies (PP, PT, PD, TT, TD, DD)


Fig. 2. Monte-Carlo experiment for the populations of viable phenotypes
Legend: Avg(Num. of viable phenotypes) vs. Millennia

Average number of phenotypes produced by deterministic selection accompanied by proportional (DP) or tournament (DT) survival, creates a distinct population of phenotypes in the cultivar in terms of numbers, which in its average lies at all evolution times (Fig. 1) than the average produced by the remaining methods of selection and survival (PP, PT, PD, TT, TD, SD). The average number of population phenotypes produced by deterministic selection accompanied by proportional (DP) or tournament (DT) survival produce a decrease of at least two phenotypes almost everywhere compared to the remaining methods (average of 15.15 for DP + DT, average of 18.18 for PP + PT + PD + TT + TD + DD) and with almost two phenotypes compared to the overall mean (17.59), with a decreasing trend of 15 phenotypes during evolution (Fig. 2).

The second examined case was of the most numerous populations which could not reveal different distributions laws (Fig. 3). On the populations presented in Fig. 3 it is remarkable the presence of four pairs in both populations (PP, PT, TD and DD) the distinct being made in each by the presence of the fifth pairs (PD and TT, respectively).


Fig. 3. Largest populations at 5\% risk being in error for the number of phenotypes during evolutions
The explanation could be found in Tab. 1, the (PP, PT, TD and DD) population had an average score of nondiscrimination ( $\mathrm{c} / \mathrm{k}$ ) of 0.422 which is even decreases with a significant amount at 0.368 when the PD sub-population was included; it was also decreased with an important amount when the TT sub-population was included. Both sub-populations proved to be significantly different (score in the pair of 0.42 - the hypothesis of belonging to the same population being rejected at a significance level of 5\%) for their inclusion in the (PP, PT, TD, DD, PD, TT) together may not be
accepted as a single population distribution, the (PP, PT, TD, DD, PD, TT) group having a membership score of identically distributed populations of 0.92 at a significance level of $5 \%$ (almost accepted - value close to 1 - but not sufficient). An important remark is that the PD (proportional selection accompanied by deterministic survival) and TT (tournament selection accompanied by tournament survival) were not identified as distinct populations under the scheme of analysis presented in Tab. 1, which made it impossible the decision of their inclusion in the group five pairs of selection-survival strategies that contains the PP, PT, TD and DD.

The analysis of Table 1 brings satisfactory answers in terms of possibilities but not in terms of probabilities. If we fix the objective to obtain the most probable partition of populations obtained by selection and survival strategies, the analysis of pairs of two is the solution (see Tab. 2 - Annex).


Fig. 4. The most probable partition of the populations of phenotypes number parameterized by selection and survival


Fig. 5. Distinct populations for the number of phenotypes:
The Monte-Carlo experiment
Legend: Avg(Num. of viable phenotypes) vs. Millennia

Thus, the combination obtained by applying the procedure described in Tab. 2 imposed the elimination of the three most week associations of population pairs: (PD, DD), (TP, TT) and (PD, PT. In this case, the solution (most probable solution) is given by the \{(DD, PP, PT, TT, TD), (DT, $\mathrm{DP})$, $\mathrm{PD}, \mathrm{TP}$ \} partition. The obtained result was graphically represented in terms of distribution of average number of phenotypes in cultivar (Fig. 4) and the average of means number of phenotype in cultivar (Fig. 5).

## CONCLUSIONS

In $7 \%$ of investigated cases, the hypothesis that the groups are from the same population could not be rejected at a significance level of $5 \%$. In $93 \%$ of cases, with a risk to be in error of $5 \%$, it could be stated that the investigated groups of selection and survival strategies are from different populations.

Tournament selection accompanied by proportional survival (TP) produce a population of distinct phenotypes in cultivar in terms of their number (its mean is situated above the mean produced by remaining methods - PP, PT, PD, TT, TD, DD - in all moments of evolution), with a mean that increase with almost one phenotype compared with all other methods.

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## ANNEX

Tab. 2
The most probable solution interpreting the results from Tab. 1

The matrix of pairs, a cell of the matrix contains 0 if with a $5 \%$ risk of being in error the pair of methods given by the row and column of the cell produce populations with distinct distribution laws and 1 otherwise.

The rows and columns of the matrix of pairs are changed so as to obtain the largest group of a compact of 1 ; one solution is the permutation on beside column.

The blocks of 1 are marked; the aim is to not have any 1 value in the neighbors of the block, which means that some identified combinations are random at a $5 \%$ risk of being in error

The elimination of values of 1 from the table should take into account the chance to be in error; analyzing the values from Table 1 it can be observed that the associations closest to the significance level of 5\% are (PD, DD) and (TP, TT), both with a c/k ratio of 1.09. Thus, these combinations are associated to chance and are eliminated.

It is easy to observe that the combination (PD, PT) hindering the partition of populations by the pair (selection method, survival method); Analyzing the value of this combination (Table 1) the assumption is confirmed, after removal of the combinations (PD, $\mathrm{DD})$ and (TP, TT) the (PD, PT) combination remained the combination with the smallest value of the $\mathrm{c} / \mathrm{k}$ ratio (1.26). The (PD, PT) combination is eliminated.

The rows and columns of the table could be permutated again for convenience.

| SS | PP | PT | PD | TP | TT | TD | DP | DT | DD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| PT | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| PD | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| TP | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| TT | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 1 |
| TD | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| DP | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 |
| DT | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 |
| DD | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| SS | DD | PP | PT | PD | TP | TT | TD | DT | DP |
| TP | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| DP | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| DT | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| PP | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PT | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| TT | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| TD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| DD | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| PD | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| SS | DD | PP | PT | PD | TP | TT | TD | DT | DP |
| DP | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - 1 | 1 |
| DT | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| TP | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| PP | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PT | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| TT | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| TD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| DD | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| PD | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| SS | DD | PP | PT | PD | TP | TT | TD | DT | DP |
| DP | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| DT | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| TP | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| PP | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PT | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 0 |
| TT | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| TD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| DD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PD | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| SS | DD | PP | PT | PD | TP | TT | TD | DT | DP |
| DP | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| DT | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| TP | 0 | 0 | 0 | 0 | - 1 | 0 | 0 | 0 | 0 |
| PP | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PT | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| TT | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| TD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| DD | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| PD | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| SS | DD | PP | PT | TT | TD | DT | DP | PD | TP |
| TP | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| PD | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| DP | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| DT | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| PP | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| PT | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| TT | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| TD | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| DD | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |

